

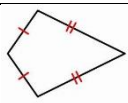



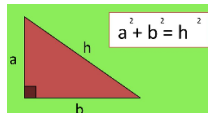
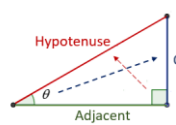
# YEAR 10 HIGHER

KNOWLEDGE ORGANISERS

Year 10 Term 1

Term		Definition
<b>Number</b>		
1	Percentage change	$Percentage\ Change = \frac{change}{original} \times 100$
2	Reverse percentages	When you are given a percentage that is not 100% and a value, and you need to work out the original value (100%). E.g. 40% = 24. So 10% = 6 So 100% = 60.
3	Percentage multiplier	A number you can multiply by to do percentage increase or decrease in one step. E.g. Increase by 7% = Multiply by 1.07 Decrease by 8% = Multiply by 0.92
4	Simple interest	Simple interest is where you calculate the first year of interest, and this is simply added on each year for a given number of years.
<b>Geometry and measures</b>		
5	Upper bound	The upper limit of what a number could be. E.g. I weight 80kg to the nearest 5kg. The upper bound would be 82.5kg
6	Lower bound	The lower limit of what a number could be. E.g. I weight 80kg to the nearest 5kg. The lower bound would be 77.5kg
7	1cm	10mm
8	1m	100cm
9	1km	1000m
10	1kg	1000g
11	1 tonne	1000kg
12	1 litre	1000ml
13	1 litre	100cl
14	1ml	1cm <sup>3</sup>
15	Speed	$Speed = \frac{distance}{time}$
16	Density	$Density = \frac{mass}{volume}$
17	Pressure	$Pressure = \frac{force}{area}$
<b>Number</b>		
18	Surd	A number that can't be simplified to remove a square root (or cube root etc). Examples: $\sqrt{2}$
19	Rationalise the denominator	"Rationalizing the denominator" is when we move a root (like a square root or cube root) from the bottom of a fraction to the top. <div style="border: 1px solid black; border-radius: 10px; padding: 5px; width: fit-content; margin-left: auto;"> <math display="block">\begin{aligned} \frac{1}{\sqrt{2}} &amp;= \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} \\ &amp;= \frac{1 \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}} \\ &amp;= \frac{\sqrt{2}}{\sqrt{2} \cdot 2} \\ &amp;= \frac{\sqrt{2}}{2} \end{aligned}</math> </div>
20	Geometric progressions	Also known as a geometric sequence, is a sequence of numbers where each term after the first is found by multiplying the previous one by a fixed, non-zero number called the common ratio. E.g. 2, 6, 18, 54,...

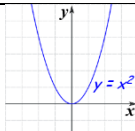
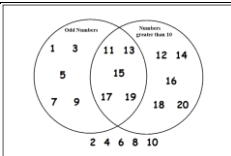
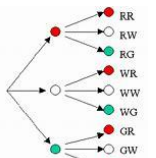
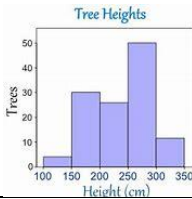
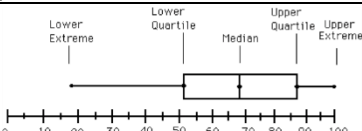
Term		Definition
<b>Statistics</b>		
1	Median	The middle of an ordered set of values.
2	Mode	The most common value in a dataset
3	Range	The difference between the largest and smallest data value.
4	Mean	The average given when you add up all the values and divide by how many values there are.
5	Quartiles	Quartiles are the values that divide a list of numbers into quarters: Put the list of numbers in order. Then cut the list into four equal parts.
6	Inter-quartile range	The interquartile range is the range between the first and third quartiles.
7	Spread	The differences between the ranges of different datasets. If the range is large, the spread is large. If the range is small, the spread is small.
8	Primary data	Data collected yourself. E.g. you design and complete a survey of students yourself.
9	Secondary data	Data collected from somewhere else that you did not collect. E.g. data from a Government census.
10	Discrete data	Data that can only take certain values. E.g. the number of students in a class, your shoe size, number of cars in the car park.
11	Continuous data	Data that can take any value. E.g. temperature, time taken to run a race, height.
12	Sampling	A sample is a selection taken from a larger group.
<b>Number</b>		
13	Integer	A whole number. A positive number, a negative number or zero but not a fraction or a decimal.
14	Roots	The root of a number X is another number, which when multiplied by itself a given number of times, equals x. For example, the square root of 100 = 10. $\sqrt{100} = 10$ . This is because $10 \times 10 = 100$ . For example, the cube root of 8 = 2. $\sqrt[3]{8} = 2$
15	Powers	A small number to tell you how many times to multiply the number by itself. It is usually at the top right of the base number. E.g. $10^6 = 10 \times 10 \times 10 \times 10 \times 10 \times 10$ E.g. $2^5 = 2 \times 2 \times 2 \times 2 \times 2$
16	Powers of 2	2,4,8,16,32,64,128,256...
17	Powers of 3	3,9,27,81,243,729,2187...
18	Powers of 4	4,16,64,256,1024,4096...
19	Powers of 5	5,125,625,3125,15625...
20	Square numbers	1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225. These form a square.
21	Fractional indices	The denominator of the fraction is the root of the number or letter, and the numerator of the fraction is the power to raise the answer to. <b>Example 1.</b> $8^{\frac{2}{3}} = (\sqrt[3]{8})^2 = 4$ <b>Example 2.</b> $16^{\frac{1}{2}} = (\sqrt{16})^1 = 4$
<b>Geometry and measures</b>		
22	Angles in a triangle	Angles in a triangle add up to 180.
23	Angle sum of a polygon	Sum of interior angles = $180 \times (n - 1)$
24	Regular polygon	A polygon is regular when all angles are equal and all sides are equal (otherwise it is "irregular").
25	Isosceles triangle	An isosceles triangle is a triangle that has two sides of equal length.
26	Equilateral triangle	An equilateral triangle is a triangle that has three sides of equal length.
27	Scalene triangle	A scalene triangle is a triangle that has three unequal length and unequal angles.
28	Right-angled triangle	A right angle triangle is a triangle with a right angle.
29	Obtuse-angled triangle	An obtuse-angled triangle is a triangle with an angle more than 90 degrees.
30	Acute-angled triangle	An acute-angled triangle is a triangle with every angle less than 90 degrees.
31	Pentagon	A pentagon is a polygon which has 5 sides.
32	Hexagon	A hexagon is a polygon which has 6 sides.
33	Octagon	An Octagon is a polygon which has 8 sides.
34	Decagon	A decagon is a polygon which has 10 sides.
35	Kite	A kite is a quadrilateral with two distinct pairs of adjacent that are congruent. The diagonals of a kite are perpendicular. 
36	Rhombus	•A rhombus is a quadrilateral with all four sides having equal length. 

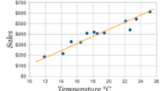
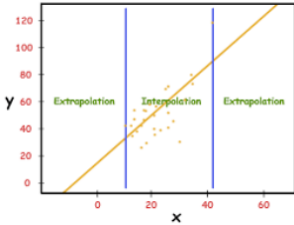
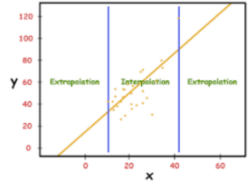
Term		Definition																																				
<b>Number</b>																																						
1	Recurring decimals	A number in which a digit or group of digits is repeated indefinitely after the decimal point. E.g. $\frac{1}{9} = 0.11111111 \dots$																																				
2	Terminating decimals	A number that contains a finite number of digits after the decimal point. E.g. $\frac{1}{2} = 0.5$																																				
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5	Nth term of Quadratic sequences	<p><b>Finding an nth term rule for a quadratic sequence</b></p> <p>For a quadratic sequence <math>an^2 + bn + c</math>                      the 2<sup>nd</sup> difference is always <math>2a</math>                      The first 1<sup>st</sup> difference is always <math>3a + b</math>                      the 1<sup>st</sup> term is always <math>a + b + c</math></p> <p>Eg find the nth term rule of the sequence 8, 14, 22, 32, ...</p> <table border="1"> <tr> <td><math>a + b + c = 8</math></td> <td>8</td> <td>14</td> <td>22</td> <td>32</td> <td>sequence</td> </tr> <tr> <td><math>\Rightarrow c = 5</math></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td><math>3a + b = 6</math></td> <td>6</td> <td>8</td> <td>10</td> <td></td> <td>1<sup>st</sup> differences</td> </tr> <tr> <td><math>\Rightarrow b = 3</math></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td><math>2a = 2</math></td> <td>2</td> <td>2</td> <td></td> <td></td> <td>2<sup>nd</sup> differences</td> </tr> <tr> <td><math>\Rightarrow a = 1</math></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> </table> <p>so the nth term rule is <math>n^2 + 3n + 4</math></p>	$a + b + c = 8$	8	14	22	32	sequence	$\Rightarrow c = 5$						$3a + b = 6$	6	8	10		1 <sup>st</sup> differences	$\Rightarrow b = 3$						$2a = 2$	2	2			2 <sup>nd</sup> differences	$\Rightarrow a = 1$					
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<b>Geometry and measures</b>																																						
10	Congruent triangles	Shapes that are exactly the same shape and size. Congruent triangles: SSS (Side, Side, Side) SAS (Side, Angle, Side) ASA (Angle, Side, Angle) RHS (Right Angle, Hypotenuse, Side)																																				
11	Similar shapes (Length, area and volume)	It is the same shape but a different size.																																				
12	Pythagoras' theorem	This is used when you have two sides of a right-angled triangle and you need to find out the third side. $a^2 + b^2 = h^2$ <div style="float: right; border: 1px solid black; padding: 5px;">  </div>																																				
13	Trigonometry	<p><b>SOHCAHTOA</b></p> <div style="display: flex; align-items: center;">  <div style="margin-left: 20px;"> <p>SOH <math>\sin \theta = \frac{\text{Opposite}}{\text{Hypotenuse}}</math></p> <p>CAH <math>\cos \theta = \frac{\text{Adjacent}}{\text{Hypotenuse}}</math></p> <p>TOA <math>\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}</math></p> </div> </div>																																				

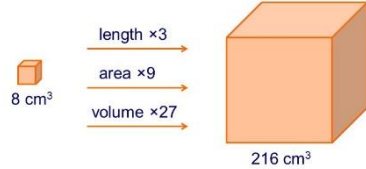
14 Exact trigonometric values

*Exact Values of Trigonometric Functions*

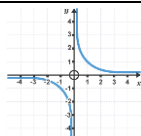
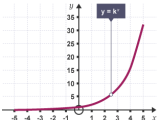



Angle ( $\theta$ )		$\sin(\theta)$	$\cos(\theta)$	$\tan(\theta)$
Degrees	Radians			
$0^\circ$	$0$	$0$	$1$	$0$
$30^\circ$	$\frac{\pi}{6}$	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$
$45^\circ$	$\frac{\pi}{4}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$	$1$
$60^\circ$	$\frac{\pi}{3}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$
$90^\circ$	$\frac{\pi}{2}$	$1$	$0$	Not Defined

Term		Definition
<b>Algebra</b>		
1	Simultaneous equations	A set of <b>equations</b> that are all satisfied by the same values of the variables.
2	Linear graph	The word <b>Linear</b> simply means straight, so if you have a <b>linear graph</b> it is a straight line graphed by the equation $y=mx+b$ where $m$ is the slope and $b$ is the $y$ intercept(the point where the line crosses the $y$ -axis).
3	Quadratic graph	A graph drafted for a quadratic equation: $ax^2 + bx + c$ $Y=x^2$ is the simplest quadratic, it's graph looks like this: 
<b>Probability</b>		
4	Randomness	Randomness is the lack of pattern or predictability in events. A random sequence of events, symbols or steps has no order and does not follow an intelligible pattern or combination.
5	Fairness	In <b>mathematics</b> we say "fair dice" when we mean that there is an equally likely chance of landing on any face.
6	Bias	Bias is a statistical term which means a systematic deviation from the true value.
7	Probability	Probability is the likelihood of something happening in the future. It is expressed as a number between 0 (impossible) and 1 (certain).
8	Mutually exclusive	Mutually exclusive outcomes cannot happen at the same time.  Flipping a coin has mutually exclusive outcomes, it can't be both heads and tails.
9	Theoretical probability	What is the probability of it happening in theory. E.g. The theoretical probability of rolling a 3 on a dice is $\frac{1}{6}$
10	Experimental probability	What was the probability of it in real life when you actually did the experiment. This will differ from the theoretical probability initially but will get closer and closer with an increasing number of trials you do.
11	Venn diagrams	A <b>diagram</b> using circles or other shapes, to show the relationship between sets. 
12	Tree diagrams	A <b>diagram</b> shaped like a <b>tree</b> used to display sample space by using one branch for each possible outcome in a probability exercise. 
13	Sample space diagrams	A sample space is the set of all possible outcomes in the experiment. It is usually denoted by the letter $S$ . Sample space can be written using the set notation, $\{ \}$ .
<b>Statistics</b>		
14	Histograms	In math, a histogram is a visual way to display frequency data using bars. A feature of histograms is that they show the frequency of continuous data. 
15	Cumulative frequency	Cumulative frequency is the running total of the frequencies.
16	Boxplots	Boxplot is a graphical representation of statistical measures like median, upper and lower quartiles, minimum and maximum data values. 
17	Primary data	Data collected yourself. E.g. you design and complete a survey of students yourself.
18	Secondary data	Data collected from somewhere else that you did not collect. E.g. data from a Government census.
19	Continuous data	Data that can take any value. E.g. temperature, time taken to run a race, height.
20	Discrete data	Data that can only take certain values. E.g. the number of students in a class, your shoe size, number of cars in the car park.
21	Quartiles	Quartiles are the values that divide a list of numbers into quarters
22	Inter-quartile range	The interquartile <b>range</b> is a measure of where the "middle fifty" is in a data set.
23	Lines of best fit	A line drawn on a scatter graphs that has roughly the same number of points above the line as below the line, passing through as many points as possible.

			
24	Interpolation	This is when you use estimate a value from within your data set. It is a useful skill to have.	
25	Extrapolation	Extrapolation is when you estimate a given value outside of your given data range. It is extremely dangerous to do this as you do not know for certain if the relationship you have identified continues before or outside of your data values.	
26	Sampling	A sample is a selection taken from a larger group.	

Term		Definition
<b>Algebra</b>		
1	Expanding double brackets	<p><b>Expand and simplify...</b></p> $(x-9)(x+6)$ $x^2 + 6x - 9x - 54$
2	Factorising quadratics	<p>A quadratic expression can sometimes be factorised into two brackets in the form of <math>(x+a)(x+b)</math> where <math>a</math> and <math>b</math> can be any term, positive, negative or zero. <math>a</math> and <math>b</math> can be found by using a product and sum method.</p>
3	Sum	Sum is the addition of a sequence of numbers
4	Product	A <b>product</b> is the answer to any multiplication problem.
5	Indices	Powers
6	Re-arranging formulae	Rearrange formulae in order to change the subject.
<b>Geometry and measures</b>		
7	Scale factors	The amount you multiply, or divide by, to get from one shape to another.
8	Similarity (Lengths, areas, volumes)	<p>It is the same shape but a different size.</p> <p><b>Volumes in similar shapes</b></p> <p>Compare the volume of the original cube and the volume of the enlarged cube:</p>  <p>The volume is enlarged by a scale factor of <math>3^3</math>.</p>
9	Volume of a cuboid	$V = b^3$
10	Volume of a cylinder	$V = \pi r^2 l$
11	Volume of a sphere	$V = \frac{4}{3} \pi r^3$
12	Volume of a pyramid	$V = \frac{1}{3} lwh$
13	Volume of a cone	$V = \frac{1}{3} \pi r^2 l$
14	"In terms of pi."	It's when you leave the answer with pi in.



Term		Definition
<b>Algebra</b>		
1	$Y = mx + c$	$y = mx + c$ is the standard form of the equation of a straight line, where 'm' is the gradient of the line and 'c' is the y-intercept.
2	Parallel lines	<b>Lines</b> are <b>parallel</b> if they are always the same distance apart (called "equidistant"), and will never meet.
3	Perpendicular lines	<b>Lines</b> that are at right angles ( $90^\circ$ ) to each other.
4	Gradient	The Gradient (also called Slope) of a straight line shows how steep a straight line is. Gradient = $\frac{\text{change in } y}{\text{change in } x}$
5	Y-intercept	The y-intercept is the point in a function where a line or curve crosses the y-axis. In other words: the value of the x-coordinate is zero.
6	Reciprocal graphs	A graph of the form $y = \frac{1}{x}$ is known as a <b>reciprocal graph</b> and once drawn, looks like this: 
7	Exponential graphs	Exponential graphs are graphs in the form $y = k^x$ . These graphs increase rapidly in the <b>y</b> direction and will never fall below the <b>x</b> -axis. An exponential graph will look like this: 
8	Solve an equation with an unknown on both sides.	$\begin{array}{r} 5x - 2 = 3x + 4 \\ -3x \quad -3x \\ \hline 2x - 2 = 4 \\ +2 \quad +2 \\ \hline 2x = 6 \\ \hline x = 3 \end{array}$
9	Cubic graph	A <b>cubic equation</b> contains only terms up to and including $x^3$ . $y = x^3$ 
10	Linear graph	The word <b>Linear</b> simply means straight, so if you have a <b>linear graph</b> it is a straight line graphed by the equation $y = mx + b$ where m is the slope and b is the y intercept (the point where the line crosses the y-axis).
11	Solve a quadratic by factorising	$\begin{aligned} 9x^2 + 30x + 25 &= 0 \\ (3x + 5)(3x + 5) &= 0 \\ 3x + 5 &= 0 \quad \text{or} \quad 3x + 5 = 0 \\ 3x &= -5 \quad \quad 3x = -5 \\ x &= -\frac{5}{3} \quad \quad x = -\frac{5}{3} \end{aligned}$
<b>Geometry and measures</b>		
12	Similar shapes	The <b>shapes</b> have the same ratios between sides.
13	Congruent	Exactly the same shape and size
14	Transformations	TERRY: Translations, Enlargements, Reflections, Rotations, Yeah!
15	Translation	A transformation where a shape is just moved left/right and up/down. It is usually written as a column vector. For example, $\begin{pmatrix} 5 \\ -2 \end{pmatrix}$ means 5 right, 2 down.
16	Enlargement	A transformation where one shapes has been enlarged by a given scale factor (can be larger or smaller). You also require a centre of enlargement.
17	Reflection	Each point in a shape appears the same distance on the opposite side of a line (the line of reflection). 
18	Rotation	A circular movement around a point. A full rotation is a turn of $360^\circ$ . 
19	Scale factor	The amount you multiply, or divide by, to get from one shape to another.
20	Surface area	The total area of the surface of a three-dimensional object.
21	Frustum	A frustum (plural: frusta or frustums) is the portion of a solid (normally a cone or pyramid) that lies between one or two parallel planes cutting it. 